

NAG Fortran Library Routine Document

F12ANF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

1 Purpose

F12ANF is a setup routine in a suite of routines consisting of F12ANF, F12APF, F12AQF, F12ARF and F12ASF. It is used to find some of the eigenvalues (and optionally the corresponding eigenvectors) of a standard or generalized eigenvalue problem defined by complex non-symmetric matrices.

The suite of routines is suitable for the solution of large sparse, standard or generalized, non-symmetric complex eigenproblems where only a few eigenvalues from a selected range of the spectrum are required.

2 Specification

```
SUBROUTINE F12ANF (N, NEV, NCV, ICOMM, LICOMM, COMM, LCOMM, IFAIL)
INTEGER          N, NEV, NCV, ICOMM(*), LICOMM, LCOMM, IFAIL
complex*16     COMM(*)
```

3 Description

The suite of routines is designed to calculate some of the eigenvalues, λ , (and optionally the corresponding eigenvectors, x) of a standard complex eigenvalue problem $Ax = \lambda x$, or of a generalized complex eigenvalue problem $Ax = \lambda Bx$ of order n , where n is large and the coefficient matrices A and B are sparse, complex and non-symmetric. The suite can also be used to find selected eigenvalues/eigenvectors of smaller scale dense, complex and non-symmetric problems.

F12ANF is a setup routine which must be called before F12APF, the reverse communication iterative solver, and before F12ARF, the options setting routine. F12AQF, is a post-processing routine that must be called following a successful final exit from F12APF, while F12ASF can be used to return additional monitoring information during the computation.

This setup routine initializes the communication arrays, sets (to their default values) all options that can be set by you via the option setting routine F12ARF, and checks that the lengths of the communication arrays as passed by you are of sufficient length. For details of the options available and how to set them see Section 10.2 of the document for F12ARF.

4 References

Lehoucq R B (2001) Implicitly Restarted Arnoldi Methods and Subspace Iteration *SIAM Journal on Matrix Analysis and Applications* **23** 551–562

Lehoucq R B and Scott J A (1996) An evaluation of software for computing eigenvalues of sparse nonsymmetric matrices *Preprint MCS-P547-1195* Argonne National Laboratory

Lehoucq R B and Sorensen D C (1996) Deflation Techniques for an Implicitly Restarted Arnoldi Iteration *SIAM Journal on Matrix Analysis and Applications* **17** 789–821

Lehoucq R B, Sorensen D C and Yang C (1998) *ARPACK Users' Guide: Solution of Large-Scale Eigenvalue Problems with Implicitly Restarted Arnoldi Methods* SIAM, Philadelphia

5 Parameters

- 1: N – INTEGER *Input*
On entry: the order of the matrix A (and the order of the matrix B for the generalized problem) that defines the eigenvalue problem.
Constraint: $N > 0$.
- 2: NEV – INTEGER *Input*
On entry: the number of eigenvalues to be computed.
Constraint: $0 < NEV < N - 1$.
- 3: NCV – INTEGER *Input*
On entry: the number of Arnoldi basis vectors to use during the computation.
 At present there is no *a priori* analysis to guide the selection of NCV relative to NEV. However, it is recommended that $NCV \geq 2 \times NEV + 1$. If many problems of the same type are to be solved, you should experiment with varying NCV while keeping NEV fixed for a given test problem. This will usually decrease the required number of matrix-vector operations but it also increases the work and storage required to maintain the orthogonal basis vectors. The optimal ‘cross-over’ with respect to CPU time is problem dependent and must be determined empirically.
Constraint: $NEV + 1 < NCV \leq N$.
- 4: ICOMM(*) – INTEGER array *Communication Array*
Note: the dimension of the array ICOMM must be at least $\max(1, LICOMM)$.
On exit: contains data to be communicated to the other routines in the suite.
- 5: LICOMM – INTEGER *Input*
On entry: the dimension of the array ICOMM as declared in the (sub)program from which F12ANF is called.
 If $LICOMM = -1$, a workspace query is assumed and the routine only calculates the required dimensions of ICOMM and COMM, which it returns in ICOMM(1) and COMM(1) respectively.
Constraint: $LICOMM \geq 140$ or $LICOMM = -1$.
- 6: COMM(*) – **complex*16** array *Communication Array*
Note: the dimension of the array COMM must be at least $\max(1, LCOMM)$.
On exit: contains data to be communicated to the other routines in the suite.
- 7: LCOMM – INTEGER *Input*
On entry: the dimension of the array COMM as declared in the (sub)program from which F12ANF is called.
 If $LCOMM = -1$, a workspace query is assumed and the routine only calculates the required dimensions of ICOMM and COMM, which it returns in ICOMM(1) and COMM(1) respectively.
Constraint: $LCOMM \geq 3 \times N + 3 \times NCV \times NCV + 5 \times NCV + 60$ or $LCOMM = -1$.
- 8: IFAIL – INTEGER *Input/Output*
On entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this parameter you should refer to Chapter P01 for details.
On exit: IFAIL = 0 unless the routine detects an error (see Section 6).
 For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then

the value 1 is recommended. Otherwise, if you are not familiar with this parameter the recommended value is 0. **When the value –1 or 1 is used it is essential to test the value of IFAIL on exit.**

6 Error Indicators and Warnings

If on entry IFAIL = 0 or –1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

IFAIL = 1

On entry, $N \leq 0$.

IFAIL = 2

On entry, $NEV \leq 0$.

IFAIL = 3

On entry, $NCV < NEV + 2$ or $NCV > N$.

IFAIL = 4

On entry, $LICOMM < 140$ and $LICOMM \neq -1$.

IFAIL = 5

On entry, $LICOMM < 3 \times N + 3 \times NCV \times NCV + 5 \times NCV + 60$ and $LICOMM \neq -1$.

7 Accuracy

Not applicable.

8 Further Comments

None.

9 Example

This example solves $Ax = \lambda x$ in regular mode, where A is obtained from the standard central difference discretization of the convection-diffusion operator $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \rho \frac{\partial u}{\partial x}$ on the unit square, with zero Dirichlet boundary conditions. The eigenvalues of largest magnitude are found.

9.1 Program Text

```
*      F12ANF Example Program Text
*      Mark 21 Release. NAG Copyright 2004.
*      .. Parameters ..
INTEGER          LICOMM, NIN, NOUT, IMON, IPOINT
PARAMETER       (LICOMM=140,NIN=5,NOUT=6,IMON=0,IPOINT=0)
INTEGER          MAXN, MAXNCV, LDV
PARAMETER       (MAXN=256,MAXNCV=30,LDV=MAXN)
INTEGER          LCOMM
PARAMETER       (LCOMM=3*MAXN+3*MAXNCV*MAXNCV+5*MAXNCV+60)
*      .. Local Scalars ..
COMPLEX *16     SIGMA
INTEGER         I, IFAIL, IFAIL1, IREVCM, N, NCONV, NCV, NEV,
+              NITER, NSHIFT, NX
*      .. Local Arrays ..
COMPLEX *16     AX(MAXN), COMM(LCOMM), D(MAXNCV,2), MX(MAXN),
```

```

+          RESID(MAXN), V(LDV,MAXNCV), X(MAXN)
  INTEGER          ICOMM(LICOMM)
*   .. External Functions ..
  DOUBLE PRECISION DZNRM2
  EXTERNAL          DZNRM2
*   .. External Subroutines ..
  EXTERNAL          AV, F12ANF, F12APF, F12AQF, F12ARF, F12ASF, ZCOPY
*   .. Intrinsic Functions ..
*   .. Executable Statements ..
  WRITE (NOUT,*) 'F12ANF Example Program Results'
  WRITE (NOUT,*)
*   Skip heading in data file
  READ (NIN,*)
  READ (NIN,*) NX, NEV, NCV
  N = NX*NX
  IF (N.LT.1 .OR. N.GT.MAXN) THEN
    WRITE (NOUT,99999) 'N is out of range: N = ', N
  ELSE IF (NCV.GT.MAXNCV) THEN
    WRITE (NOUT,99999) 'NCV is out of range: NCV = ', NCV
  ELSE
    IFAIL = 0
    CALL F12ANF(N,NEV,NCV,ICOMM,LICOMM,COMM,LCOMM,IFAIL)
    IF (IPOINT.NE.0) THEN
*   Use pointers to Workspace in calculating matrix vector products
*   rather than interfacing through the array X
      CALL F12ARF('POINTERS=YES',ICOMM,COMM,IFAIL)
    END IF
    IREVCM = 0
    IFAIL = -1
20   CONTINUE
    CALL F12APF(IREVCM,RESID,V,LDV,X,MX,NSHIFT,COMM,ICOMM,IFAIL)
    IF (IREVCM.NE.5) THEN
      IF (IREVCM.EQ.-1 .OR. IREVCM.EQ.1) THEN
*   Perform matrix vector multiplication y <--- Op*x
        IF (IPOINT.EQ.0) THEN
          CALL AV(NX,X,AX)
          CALL ZCOPY(N,AX,1,X,1)
        ELSE
          CALL AV(NX,COMM(ICOMM(1)),COMM(ICOMM(2)))
        END IF
      ELSE IF (IREVCM.EQ.4 .AND. IMON.NE.0) THEN
*   Output monitoring information
        CALL F12ASF(NITER,NCONV,D,D(1,2),ICOMM,COMM)
        WRITE (6,99998) NITER, NCONV, DZNRM2(NEV,D(1,2),1)
      END IF
      GO TO 20
    END IF
    IF (IFAIL.EQ.0) THEN
*   Post-Process using F12AQF to compute eigenvalues/vectors.
      IFAIL1 = 0
      CALL F12AQF(NCONV,D,V,LDV,SIGMA,RESID,V,LDV,COMM,ICOMM,
+          IFAIL1)
*
      WRITE (NOUT,99996) NCONV
      DO 40 I = 1, NCONV
        WRITE (NOUT,99995) I, D(I,1)
40     CONTINUE
      ELSE
        WRITE (NOUT,99997) IFAIL
      END IF
    END IF
    STOP
*
99999 FORMAT (1X,A,I5)
99998 FORMAT (1X,'Iteration',1X,I3,',', No. converged =',1X,I3,',', norm o',
+   'f estimates =',E16.8)
99997 FORMAT (1X,' NAG Routine F12APF Returned with IFAIL = ',I6)
99996 FORMAT (1X,' The ',I4,' Ritz values of largest magnitude are:',/)
99995 FORMAT (1X,I8,5X,'( ',F12.4,', ',F12.4,', )')
  END
*

```

```

SUBROUTINE AV(NX,V,W)
*   .. Scalar Arguments ..
INTEGER    NX
*   .. Array Arguments ..
COMPLEX *16  V(NX*NX), W(NX*NX)
*   .. Local Scalars ..
COMPLEX *16  H2
INTEGER      J, LO
*   .. External Subroutines ..
EXTERNAL    TV, ZAXPY
*   .. Intrinsic Functions ..
INTRINSIC   CMPLX
*   .. Executable Statements ..
H2 = CMPLX(-(NX+1)*(NX+1),KIND=KIND(H2))
*
CALL TV(NX,V(1),W(1))
CALL ZAXPY(NX,H2,V(NX+1),1,W(1),1)
*
DO 20 J = 2, NX - 1
    LO = (J-1)*NX
    CALL TV(NX,V(LO+1),W(LO+1))
    CALL ZAXPY(NX,H2,V(LO-NX+1),1,W(LO+1),1)
    CALL ZAXPY(NX,H2,V(LO+NX+1),1,W(LO+1),1)
20 CONTINUE
*
LO = (NX-1)*NX
CALL TV(NX,V(LO+1),W(LO+1))
CALL ZAXPY(NX,H2,V(LO-NX+1),1,W(LO+1),1)
*
RETURN
END
*
SUBROUTINE TV(NX,X,Y)
*   Compute the matrix vector multiplication  $y \leftarrow -T*x$  where T is a nx
*   by nx tridiagonal matrix.
*   .. Parameters ..
COMPLEX *16  RHO
PARAMETER    (RHO=(1.0D+2,0.0D+0))
*   .. Scalar Arguments ..
INTEGER      NX
*   .. Array Arguments ..
COMPLEX *16  X(NX), Y(NX)
*   .. Local Scalars ..
COMPLEX *16  DD, DL, DU, H, H2
INTEGER      J
*   .. Intrinsic Functions ..
INTRINSIC    CMPLX
*   .. Executable Statements ..
H = CMPLX(NX+1,KIND=KIND(DD))
H2 = H*H
DD = (4.0D+0,0.0D+0)*H2
DL = -H2 - (5.0D-1,0.0D+0)*RHO*H
DU = -H2 + (5.0D-1,0.0D+0)*RHO*H
*
Y(1) = DD*X(1) + DU*X(2)
DO 20 J = 2, NX - 1
    Y(J) = DL*X(J-1) + DD*X(J) + DU*X(J+1)
20 CONTINUE
Y(NX) = DL*X(NX-1) + DD*X(NX)
RETURN
END

```

9.2 Program Data

F12ANF Example Program Data
10 4 20 : Vaues for NX NEV and NCV

9.3 Program Results

F12ANF Example Program Results

The 4 Ritz values of largest magnitude are:

1	(716.1973	,	-1029.5838)
2	(687.5834	,	-1029.5838)
3	(716.1973	,	1029.5838)
4	(687.5834	,	1029.5838)
